# Failure Intensity Determination for Renewal Doubling System with Parallel Redundancy

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Abstract - The problem of failure intensity determination for renewal doubling system with parallel redundancy is considered.

Keywords - Reliability, Failure Intensity, Markov Analysis, Parallel Redundancy, Doubling.

#### I. INTRODUCTION

The failure intensity is ratio of mean number renewal system failures for infinitesimal life to this life quantity. This index shows system upstate leaving frequency. Both availability and failure intensity are characterized renewal system reliability property.

#### **II. SYSTEM RELIABILITY MODELS**

The method for failure intensity calculation for renewal doubling system with parallel redundancy that based on Markov reliability model is suggested.

The system functions by such maintainability algorithm. It's situated in up state  $S_1$  (fig. 1) at the beginning.

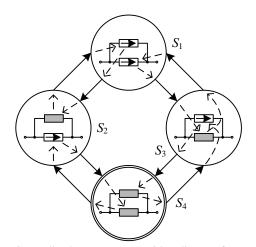


Fig.1. Generalized state space transition diagram for renewal doubling system with parallel redundancy

In this state both components are functioning properly and they life is given by phase-type failure model  $R_1(t)$ . If one component downs, then system cross to  $S_3$  state, else – cross to  $S_2$  state. It's assumed that technical diagnostics facilitates are ideal. This means that component failure is tested instantaneously. After repair failure component is "as good as new". At  $S_2$  and  $S_3$  up states one component is operable and other - not operable. Such component life is given by phasetype failure model  $R_1(t)$  too and time repair is given by exponential maintainability model  $M_1(t)$ .

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If good component downs, then system crosses to  $S_4$  state, and if faulty component ups, then system returns to  $S_1$  state. At  $S_4$  down states both component are not operable and time repair are given by exponential maintainability model  $M_1(t)$ . If one component ups, than system return to  $S_2$  or  $S_3$  upstate.

For considered system Markov reliability model was formed using phase-type distributions and state space extending. More about this approach see in [1, 2].

System failure intensity  $z_1(t)$ , solid bold curve 1 (fig. 2) is determined as sum of product transition intensity, that shift system from up to down state, and such upstate system probability function.

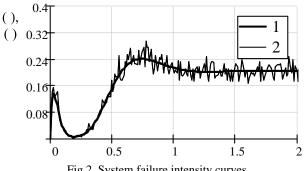


Fig.2. System failure intensity curves

For result accuracy verification system failure intensity  $z_2(t)$ , solid curve 2 (fig. 2) was determined by Monte-Carlo reliability model.

### **III. CONCLUSION**

Curve 1 is agrees with curve 2 in tolerant limits. Curve 2 is distorted by Monte-Carlo method noise. Integral mean root error between 1 and 2 failure intensity curves for 50000 Monte-Carlo iterations is about 0.02. Simulation duration for extended state space Markov reliability model is less then simulation duration for Monte-Carlo reliability model more than 500 times. Such, using homogeneous extended state reliability model, space Markov failure intensity determination method for renewal doubling system with parallel redundancy is proposed.

#### REFERENCES

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