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PREDICTION OF TRIBOLOGICAL PROPERTIES OF STRUCTURAL STEELS USING ARTIFICIAL NEURAL NETWORKS

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Abstract. The effect of quenching temperature on wear resistance of 40Kh steel after tempering has been investigated. It was found that compared to standard heat treatment, quenching from 1050 °C and high temperature tempering increase its tribological characteristics. The character of fracture of the contacting surfaces was studied. It was shown that in the specimens quenched from 860 °C and tempered, the fracture of the contact surface occurs by the mechanisms of smooth splitting and delamination with plastic deformation. Increasing the quenching temperature to 1050 °C along with high temperature tempering changes the character of the contact surface destruction. The areas with a distinctive microstructure appear on the surface exhibiting substantially higher wear resistance during friction as compared to the surrounding volume. The structural-geometrical parameters characterizing the roughness and bearing capacity of the contact interaction surface were analyzed. It was found that increasing the quenching temperature to 1050 °C allows to reduce the surface roughness and increase the bearing capacity. Using the methods of optical and transmission electron microscopy, the peculiarities of forming the microstructure of the investigated steel were studied, depending on the temperature conditions of the thermal treatment. It was shown that raising the quenching temperature to 1050 °C increases the austenitic grain size, enhances non-uniformity of carbon distribution, which leads to the formation of large needle-shaped crystals of lath martensite with microtwin boundaries inside. This, in turn, promotes the formation at high tempering of non-uniformly distributed aggregates of coarse carbides at these microtwin boundaries. The aggregates form areas of microstructure with increased resistance to plastic deformation processes. That is, the morphology of the carbide phase is one of the main factors that determine the tribological characteristics of steel, namely roughness, structural-geometrical parameters and bearing capacity of the surface. The expediency of using artificial neural networks for prediction of tribological properties of structural steels was shown. According to the results of modeling the structural-geometrical parameters of the surface and the roughness characteristics, the bearing capacity of the 40Kh steel surface during friction was predicted.

Keywords: steel microstructure, carbide phase, wear resistance, surface bearing capacity, structural-geometrical parameters of the surface, neural network modeling.

Introduction. Problem Statement

The development of mechanical engineering requires an increase in the power, reliability, and durability of machine parts and mechanisms under their conditions of operation in gas and liquid environments, at low and high temperatures.

The available data on the physical and mechanical properties of the materials make it possible to provide sufficient strength for machine parts with a guarantee of failure-free operation. But the most common

cause of failure of machine parts is not complete fracture, but wear and damage to the working surfaces due to friction. It is the damaging of the surface that disrupts the operation mode for the parts of the friction units, causes additional loads, percussion in the joints and vibrations, causing unacceptable noise, sticking and jamming, which in the end causes accidents.

80–85 % of machines and mechanisms fail due to wear of parts, and having them idle when repairing moving joints results in reduced efficiency by 15–20 % [1–6]. Consequently, the durability, reliability and lifetime of machines are in many cases related to the wear resistance of the materials from which they are made [7–10]. Therefore, minimization of wear is one of the central segments in solving problems such as energy savings, reducing outgoings of material, and ensuring the reliability and safe operation of mechanical systems. In this regard, further research in the field of tribotechnical materials science, which can deepen existing and find new ways to reduce friction losses and wear by increasing the wear resistance of machine parts and mechanisms, is of particular importance. This confirms the need to study the general patterns of fracture in the conditions of contact interaction and their relationship with the features of structure formation during the heat treatment of parts. The experience gained here allows to significantly reducing the cost of restoring and repairing mechanisms and machines, significantly improving their safety and productivity [11–14].

At the same time, the process of tribological research in most cases requires the testing of a large number of specimens, the use of expensive experimental equipment, and the interpretation of results, which is often difficult. Therefore, to predict the workability of materials under friction and to control the structural-phase state of the contact surfaces which would provide the required level of physical and mechanical properties, it is important to combine the results of experiments with modern computer simulation.

Review of Modern Information Sources on the Subject of the Paper. Objectives and Problems of Research

Currently, artificial neural networks (ANNs) are increasingly used to solve a wide range of practical tasks, such as process modeling, predicting, regulation and optimization of decision-making, analysis of property change monitoring, pattern recognition, signal processing, control, etc. [15–17]. ANN is a software or hardware embodiment of mathematical models that are built on the principle of the organization and operation of biological neural networks, namely nerve cell networks of a living organism, and is a computer technology closely related to neurophysiology, mathematics, statistics, physics, and engineering.

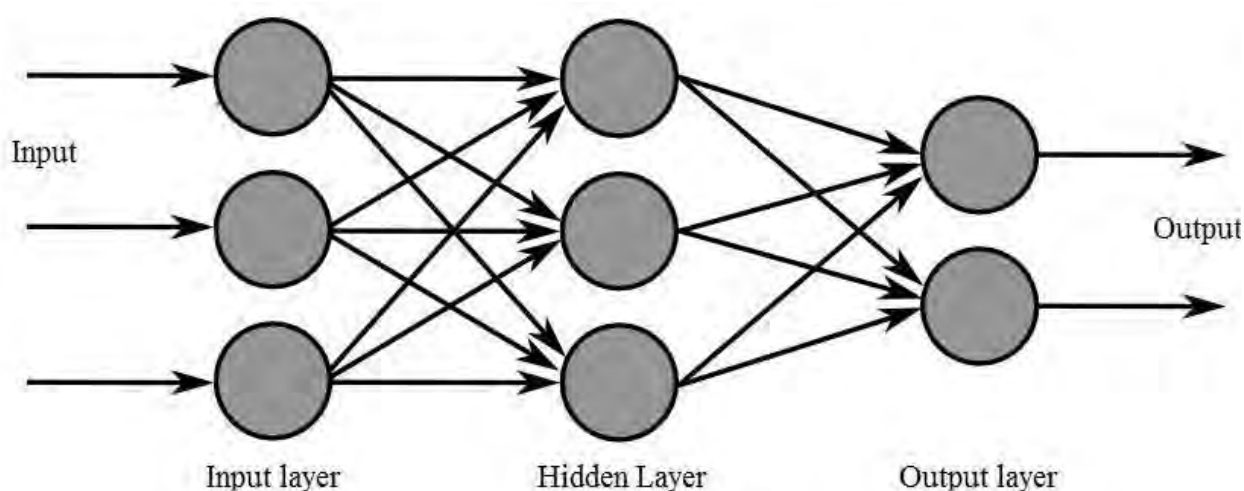


Fig. 1. Scheme of building a typical artificial neural network [18]

The scheme of the typical construction of an ANN is shown in Fig. 1. Neural networks are groups of neurons in the form of layers interconnected in a specific way. Although there are networks that contain

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only one layer or even one element, most implementations use networks that contain at least three types of layers: input, hidden and output. Input layer neurons receive experimental data either from input files or directly from electronic sensors. The output layer sends the information directly to the external environment to a secondary computer process or another device. Between these two layers may be one or more hidden ones that contain a large number of differently connected neurons. The inputs and outputs of each of the hidden neurons are connected to all other neurons. The type of connection between neurons has a great impact on the operation of the network and there are two types: the first, which excites neurons, the so-called mechanism of summation, and the second, which transmits inhibiting signals, called the mechanism of subtraction [18].

The direction of connection from one neuron to another is an important aspect of neural network functioning. In an ANN of direct propagation, each neuron of the hidden layer receives signals from the neurons of the previous one and, after performing operations on the signals, transmits its output to the neurons of the next layers, providing the signal forward to the output. In addition to direct propagation networks, in which the signal propagates strictly from the input layer to the output layer, there are feedback (backpropagation) networks [19] in which the output of neurons is directed to neurons of the previous layer.

The most important feature of an ANN is the ability to learn from examples, numerical experimental data, or environmental parameters. ANN learning is a process in which the neural network parameters are adjusted by modeling the environment into which the network is embedded. As a result of the learning, the architecture of the neural networks is adapted, their efficiency is increased, and the algorithm for solving real tasks is optimized. The type of learning is determined by how to adjust these parameters. This definition of the learning process involves the following sequence of actions [17]:

- Excitation results (data) come from the external environment to ANN.
- As a result, the ANN's free parameters change, that is, its setting is changed.
- After changing the internal architecture ANN responds to the excitation in another way.

But at present, there is no universal learning algorithm that is suitable for all ANN types. There is only a set of tools, represented by a large number of learning algorithms, each with its disadvantages and advantages [17].

Up to now, many variants of ANN and their modifications have been created, which are increasing every year [20]. Since neural networks are a sufficiently efficient apparatus for modeling complex processes and have universal approximating properties, it makes sense to use them to solve prediction tasks [21]. This contributes to their successful use for solving a wide range of applied tasks of classification, control, managing and connection [22–25], in digital technology [26], systems of technical vision [27, 28], economics [29, 30], with speech recognition [31, 32], design of Intelligent Home systems [33], implementation of intelligent agents for information collection and virus search [34–37], for the analysis of electromechanical systems [38, 39], etc. Most existing ANN software packages allow the user to add, subtract, and manage connections as desired and can be made both exciting and inhibiting by constantly adjusting the connection settings. An important factor in the network operation is the choice of the actual number of neurons and the necessary connections between them [40].

The solution of the vast majority of materials science tasks is based on the study of microstructure, phase composition, the complex of mechanical properties of machine parts, as well as their change during operation and depending on its conditions. Given this, the authors of the works [41, 42] have shown that one of the most promising tools for solving applied problems of material science is the use of computer neural network modeling. Therefore, the purpose of this work was to determine the possibility of using artificial neural networks to predict the tribological properties of structural materials.

Main Material Presentation

The object of research was industrially smelted structural steel 40Kh of the following chemical composition: 0.41 % C, 0.45 % Mn, 0.33 % Si, 0.98 % Cr, 0.054 % Ni, 0.03 % S, 0.03 % P. Considering the

influence of temperature-time conditions of heat treatment on the morphology of the martensite and carbide phases, which influences the mechanical characteristics of steels [43, 44], the quenching of the investigated steels was carried out in oil from a standard temperature of 860 °C [45] and 1050 °C.

The wear resistance was determined on a 2070 CMT-1 machine according to the “disk-pad” scheme in the mode of dry sliding friction at a load of 300 N and a sliding speed of 0.5 m/s. The test time was 10 hours. The counter-body material was steel 45 with a hardness of 50 – 52 HRC. Wear resistance was evaluated hourly by weight loss. The microstructure was examined by optical and transmission electron microscopy. Stereometric studies of surface microtopography were performed on a computerized Rank Taylor Hobson stereometric profilometer with a Taliscan scanning head with a quantization step of 1–2 μm. The structure of the contact interaction surface was studied by scanning electron microscopy (SEM). The hardness was measured by the Brinell method, and the microhardness by the scratching method on the PMT-3 microhardness tester under a load of 20 g with a step of 2–4 μm according to the method defined in [46].

Quenching from 1050 °C compared to standard heat treatment reduces the Brinell hardness of tempered 40Kh steel from 2636 to 2499 MPa. At the same time, tribological tests showed (Table 1) that, notwithstanding the decrease in hardness, raising the quenching temperature to 1050 °C decreases the wear intensity of the specimens of the investigated steel from 3.719 to 3.012.

Table 1

Dependence of the weight wear intensity I_m on the quenching temperature of 40Kh steel after tempering

Quenching temperature t , °C	$I_m \cdot 10^{-8}$	Brinell hardness, MPa
860	3.719	2636
1050	3.012	2499

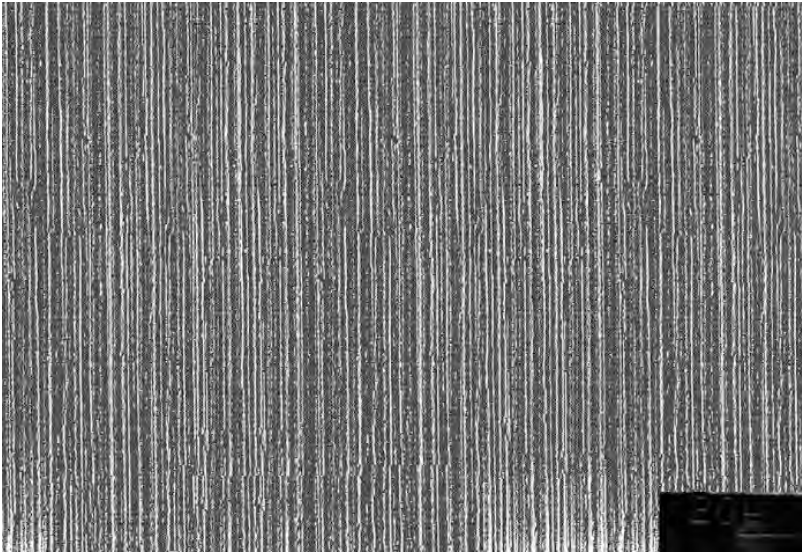
SEM studies of the contact surface before the wear test showed (Fig. 2, *a*) that it is independent of the heat treatment conditions and is identical for both studied quenching temperatures.

Contact interaction promotes the formation of zones of local plastic deformation on the friction surface of 40Kh steel specimens tempered after quenching from 860 °C. These zones are elongated in the direction of the counter-body motion (Fig. 2, *b*). On the surface, one can see scratches, chips, and the dimples as signs of peeling of carbides and their separation from the matrix, which are elongated in the direction of sliding. The fracture of the friction surface occurs by mechanisms of smooth delamination with plastic deformation and splitting.

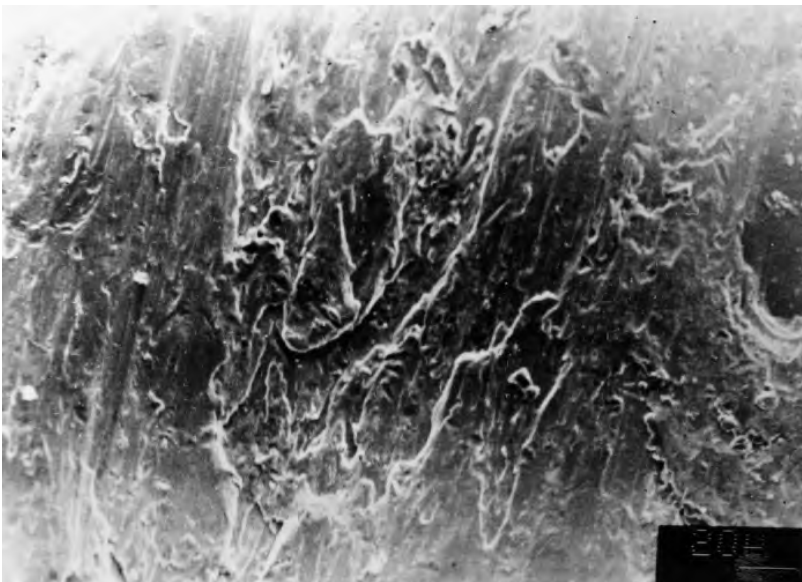
Increasing the quenching temperature to 1050 °C with high temperature tempering changes the character of the surface of the contact interaction, which becomes non-uniform (Fig. 2, *c*). This change is obviously related to the peculiarities of the fracture processes occurring in individual parts of the surface. In most of the contact area, there are local sections with dimensions that do not coincide with any elements of the microstructure. The fracture in these places occurs by smooth delamination with signs of plastic deformation (scratches, cleavage, tearing away of carbides from the matrix and their crumbling).

This indicates that the plastic deformation of the sub-surface layers, which are apparently saturated with uniformly distributed carbide inclusions of various sizes, is responsible for the formation of such sections. Larger carbides crumble from the surface and may subsequently cause its microfracture. The smaller ones dissociate into the surrounding matrix while the plastic deformation. In this case, the situation corresponds to the peculiarities of fracture of the contact surface of the 40Kh steel specimens after quenching from 860 °C and high temperature tempering.

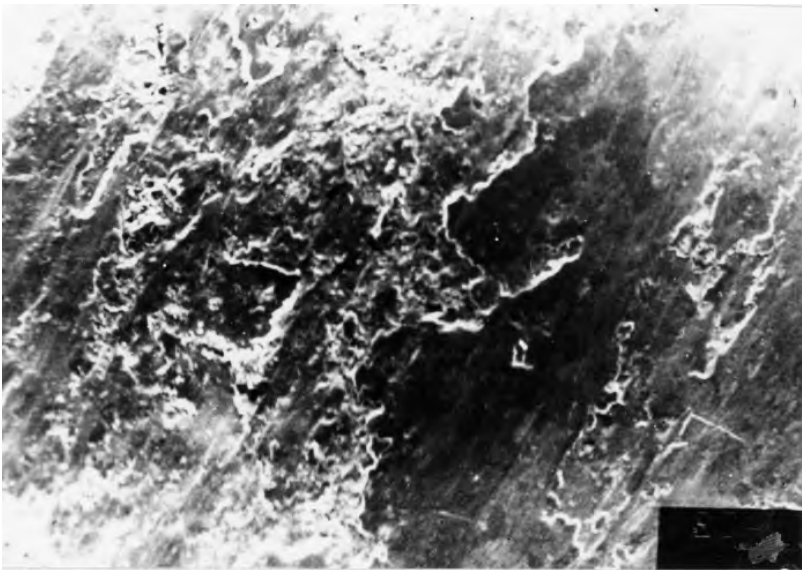
In other sections of the contact surface, the total area of which is about 15 % of the total contact surface area, the fracture is also ductile. However, the microstructure of such sections has a much greater resistance to fracture upon contact interaction. This is obviously related to the change in the morphology of the carbides, which in this case have a larger aggregation and size, and also stronger bonds to the matrix.



a



b



c

Fig. 2. Contact surfaces of 40Kh steel specimens after quenching from a temperature 860 (a, b) and 1050 °C (b) and tempering at 600 °C: (a) after grinding before tribological tests; (b, c) after tribological tests

Stereometric studies of friction surface microtopography gave structural-geometrical parameters (Table 2) characterizing the roughness, as well as discrete asymmetric images of the surface of specimens of the investigated steel after grinding of the specimens quenched from 860 °C and tempered at 600 °C (Fig. 3, a) and after tribological tests of the specimens quenched from 860 °C and 1050 °C, respectively, and tempered at 600 °C (Fig. 3, b, c). The obtained results indicate that the initial roughness of the parts of the moving joints does not depend on the conditions of heat treatment, i.e. it is similar for both investigated quenching temperatures. Thus, the initial roughness does not determine the geometry of the surface in the contact area formed during friction. This confirms the results of works [47–49], in which it is shown that under different conditions and in different friction couples after pre-working, regardless of the initial roughness, the same, equilibrium roughness is established (Fig. 4).

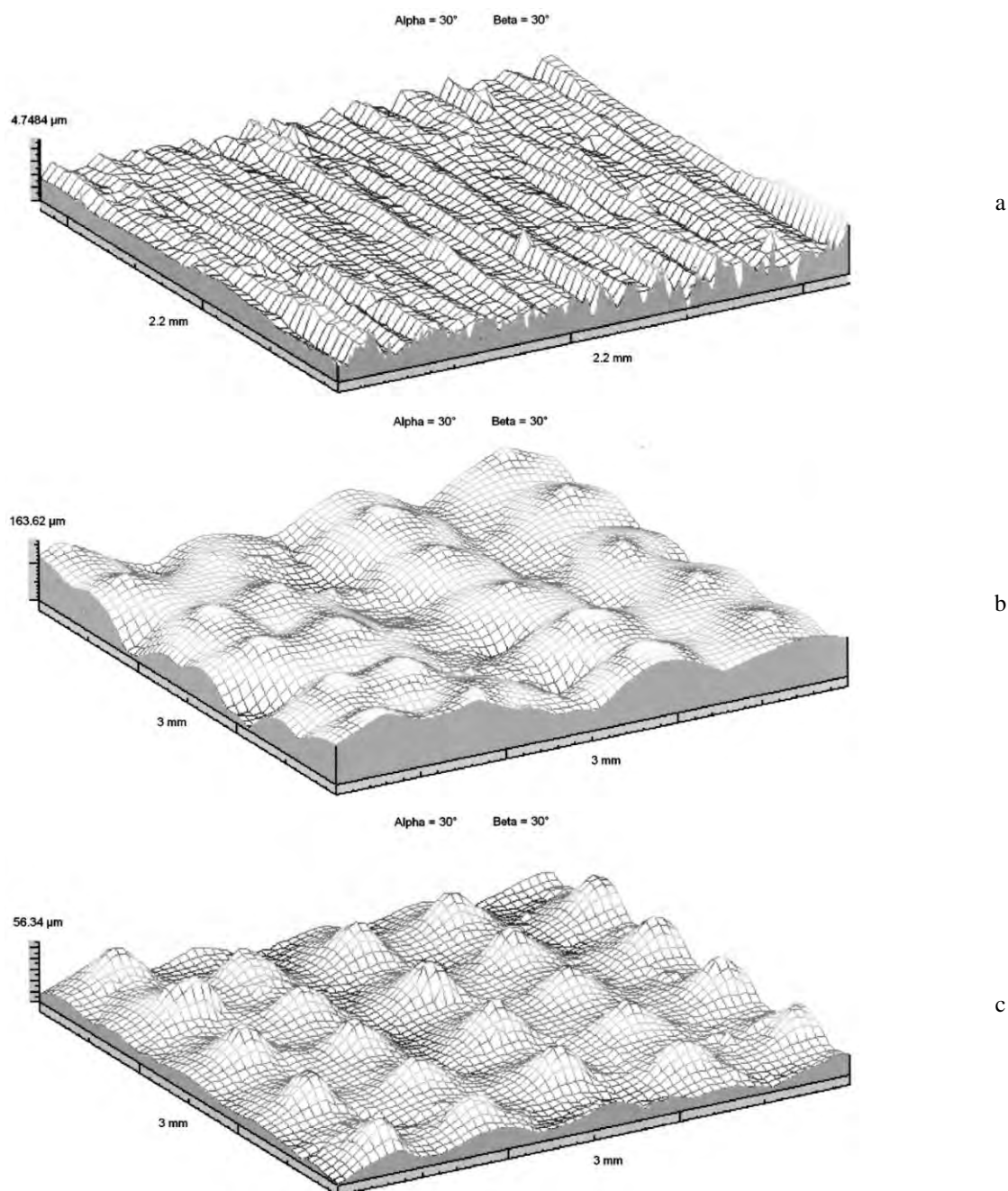


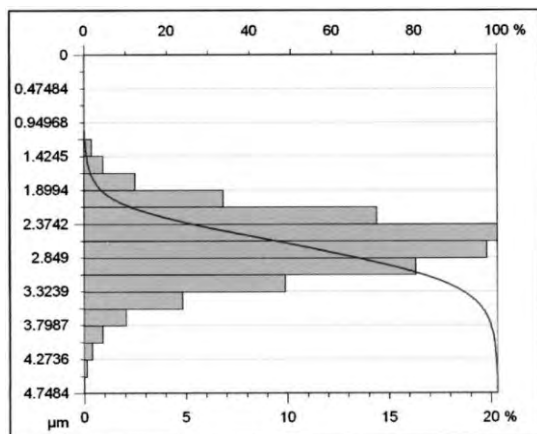
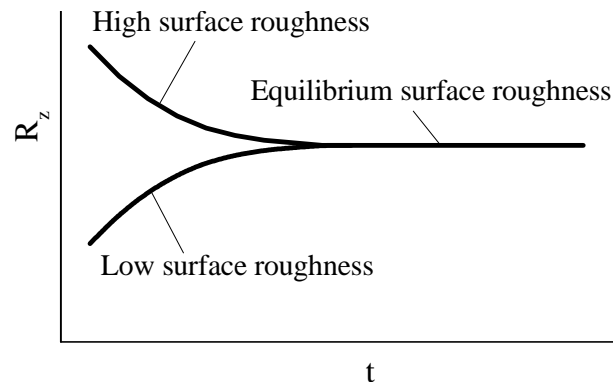
Fig. 3. Discrete asymmetric images of the 40X steel specimens surface: (a) after grinding of the specimens quenched from 860 °C and tempered at 600 °C; (b, c) after tribological tests of the specimens quenched from 860 °C and 1050 °C, respectively, and tempered at 600 °C

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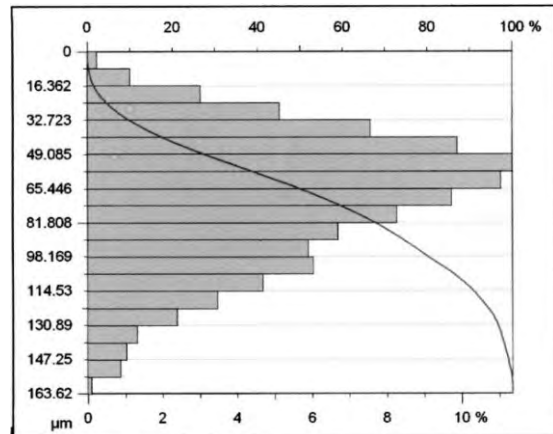
Carrying out the analysis of certified parameters according to ISO 13565 [50, 51] for the studied surfaces made it possible to construct curves that determine their “bearing capacity” (Fig. 5). As can be seen, the maximum bearing capacity has a polished surface (Fig. 5a). But in the process of operation, due to the formation of equilibrium roughness, the capacity changes and, as in the case of roughness, its certain equilibrium value is established.

Comparison of the samples after tribological tests showed that raising the quenching temperature to 1050 °C (Fig. 3, c; 5, c; Table 2) contributes to the reduction of the roughness and the increase of the bearing capacity of the surface of the tempered 40Kh steel specimens during friction as compared to the specimens quenched from 860 °C (Fig. 3, b; 5, b; Table 2).

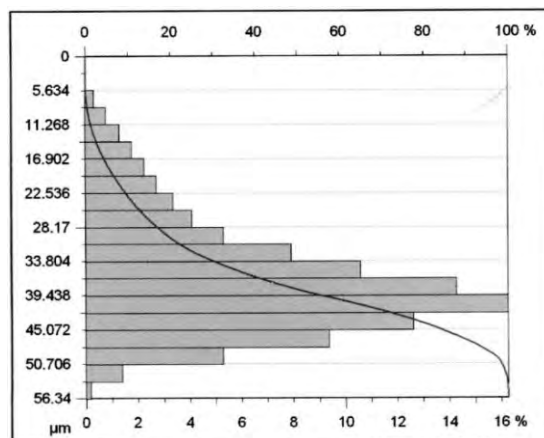
Fig. 4. Effect of operating time (t) on the average distance based on the ten highest peaks and lowest valleys (R_z) of the surfaces of moving joint parts [48]



a



b



c

Fig. 5. Amplitude distribution of the surface profile with superimposed image of the bearing surface of 40Kh steel specimens: (a) after grinding before tribological tests of the specimens quenched from 860 °C and tempered at 600 °C; (b) after tribological tests of the specimens quenched from 860 °C and tempered at 600 °C; (c) after tribological tests of the specimens quenched from 1050 °C and tempered at 600 °C

**Structural-geometrical surface parameters (according to ISO 4288)
of the studied 40Kh steel specimens before and after the wear test**

Parameter	State		
	before the wear test	after the wear test	
	Quenching temperature, °C		
	860	860	1050
Amplitude parameters			
Sa	0.3697 μm	24.879 μm	7.1195 μm
Sq	0.47311 μm	30.475 μm	9.1392 μm
Sp	2.6779 μm	69.946 μm	16.647 μm
Sv	2.0705 μm	93.669 μm	19.7 μm
St	4.7484 μm	163.62 μm	58.34 μm
Ssk	-0.14415	-0.43799	0.91073
Sku	3.7171	2.647	3.5548
Sz	4.0711 μm	154.47 μm	48.159 μm
Area & volume parameters			
STp	0.1 % (1 μm under the highest peak)	0 % (1 μm under the highest peak)	
SHTp	0.75658 μm (20 % – 80 %)	54.729 μm (20 % – 80 %)	14.141 μm (20 % – 80 %)
Smmr	0.0020705 mm ³ /mm ²	0.093669 mm ³ /mm ²	0.0197 mm ³ /mm ²
Smvr	0.0026779 mm ³ /mm ²	0.069946 mm ³ /mm ²	0.036641 mm ³ /mm ²
Spatial parameters			
SPc	0 pks/mm ² (1 μm ; 10 μm)	0.55556 pks/mm ² (1 μm ; 10 μm)	
Sds	1583.5 pks/mm ²	29.222 pks/mm ²	255.33 pks/mm ²
Str	0.023256	0.17898	0.66797
Sal	0.017221 mm	0.2636 mm	0.18805
Std	1.5 °	63.5 °	76.0 °
Hybrid parameters			
Sdq	0.048588 μm/μm	0.24774 μm/μm	0.12739 μm/μm
Ssc	0.007393 1/μm	0.041156 1/μm	0.01879 1/μm
Sdr	0.11783 %	3.0112 %	0.79474 %
Functional parameters, 0.5 μm			
Sk	1.0319 μm	47.647 μm	19.283 μm
Spk	0.3671 μm	15.239 μm	14.634 μm
Svk	0.41572 μm	16.134 μm	4.3158 μm
Sr ₁	9.2 %	10.527 %	16.729 %
Sr ₂	90.9 %	88.337 %	92.829 %
Functional parameters			
Sbi	0.24301	1.2017	0.5166
Sci	1.4447	1.353	2.0287
Svi	0.12567	0.1215	0.68628

The obtained result confirms the data of SEM studies (Fig. 2), as well as the conclusions of the works of many authors, in particular [52, 53], which showed that the decrease of altitude parameters of roughness, increase of length of supporting curves of friction surfaces, optimization of areas of peaks and valleys for given friction conditions indicate that structures providing increased resistance of the material to the processes of tribodestruction are formed in the active layer. That is, obtained after quenching from elevated

temperatures, the microstructure of 40Kh steel contributes to the formation of a more optimal contact surface relief than after standard heat treatment. Obviously, both the equilibrium roughness and the bearing capacity of the contact surface depend on the microstructure of the test specimens.

Microstructure studies have shown that quenching from a temperature of 860 °C leads to the formation of austenite grains with an average diameter of 21.5 μm in 40Kh steel (Fig. 6, *a*). As the quenching temperature rises to 1050 °C, the grains whose size varies from 35 to 270 μm are observed in the structure of the investigated steel, and the average diameter is 102 μm (Fig. 6, *b*).

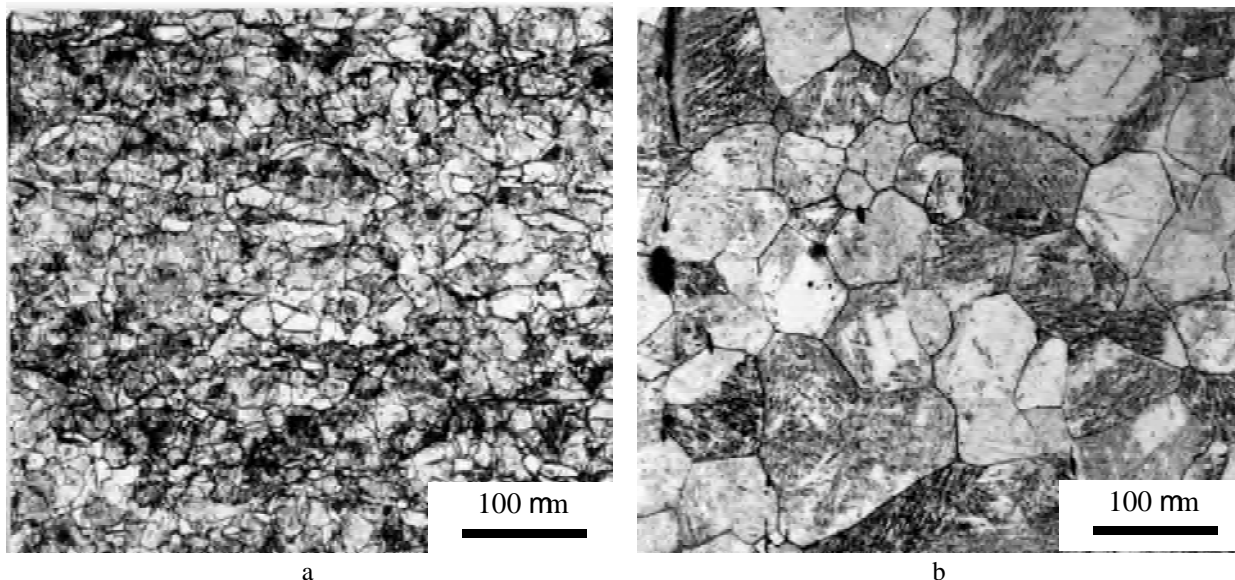


Fig. 6. The microstructure of 40Kh steel after quenching from a temperature 860 (*a*) and 1050 °C (*b*)

Transmission electron microscopic studies revealed martensite of two types, namely packet lath one and needle-shaped one with microtwins inside, in the microstructure of 40Kh steel specimens quenched from various temperatures (Fig. 7). At the same time, with increasing the quenching temperature to 1050 °C, due to carbon redistribution during the austenitization and grain growth, the size and volume fraction of needle-shaped crystals increase (Fig. 7, *b*) [54].

Analysis of the carbide phase distribution in the tempered specimens showed that after quenching from 860 °C and high temperature tempering, the equiaxial carbides with an average diameter of 0.05 μm were uniformly distributed in the steel structure. Deposition of carbides occurs mainly at the boundaries of the packet martensite cells formed during the tempering and the boundaries of the former needle-shaped martensite crystals, whose width slightly exceeds the cross-section of the martensite laths (Fig. 8, *a*). That is, the microstructure of 40Kh steel after the standard heat treatment is statistically homogeneous in the microstructural elements. This determines the homogeneity of the contact interaction surface, as discussed above (Fig. 2, *b*).

As the quenching temperature rises to 1050 °C, large crystals of needle-shaped martensite with microtwins inside whose cross-section significantly exceeds the width of the martensite laths of other morphology are formed along with packet martensite. When this structure is tempered, equiaxial carbides are deposited at the boundaries of the former packet martensite laths, as in the case of quenching from 860 °C. But as the temperature of austenitization rises and the width of the laths increases, the tempered microstructure cells become larger and the length of the substructural boundaries decreases. This results in a larger size and a decrease in the number of carbide inclusions, the average diameter of which is 0.055 μm, although no carbide-free microstructure sections are observed.

During tempering of the needle-shaped martensite, carbide formation occurs inside the crystals at the microtwin boundaries, resulting in a large number of clusters of coarse carbides of elongated shape up to 0.2 μm in size (Fig. 8, *b*). The size and location of carbides determine their increased resistance to

dissociation during the plastic deformation. The microvolumes of material with such morphology are characterized by the presence of internal micro-distortions having higher mechanical properties, in particular, microhardness and higher wear resistance as compared to the surrounding microstructure. The mentioned difference in the morphology of the carbide phase determines the heterogeneity both in structure and in mechanical properties of the contact interaction surface of 40Kh steel tempered after quenching from 1050 °C, which confirms the results of SEM studies (Fig. 2, c).

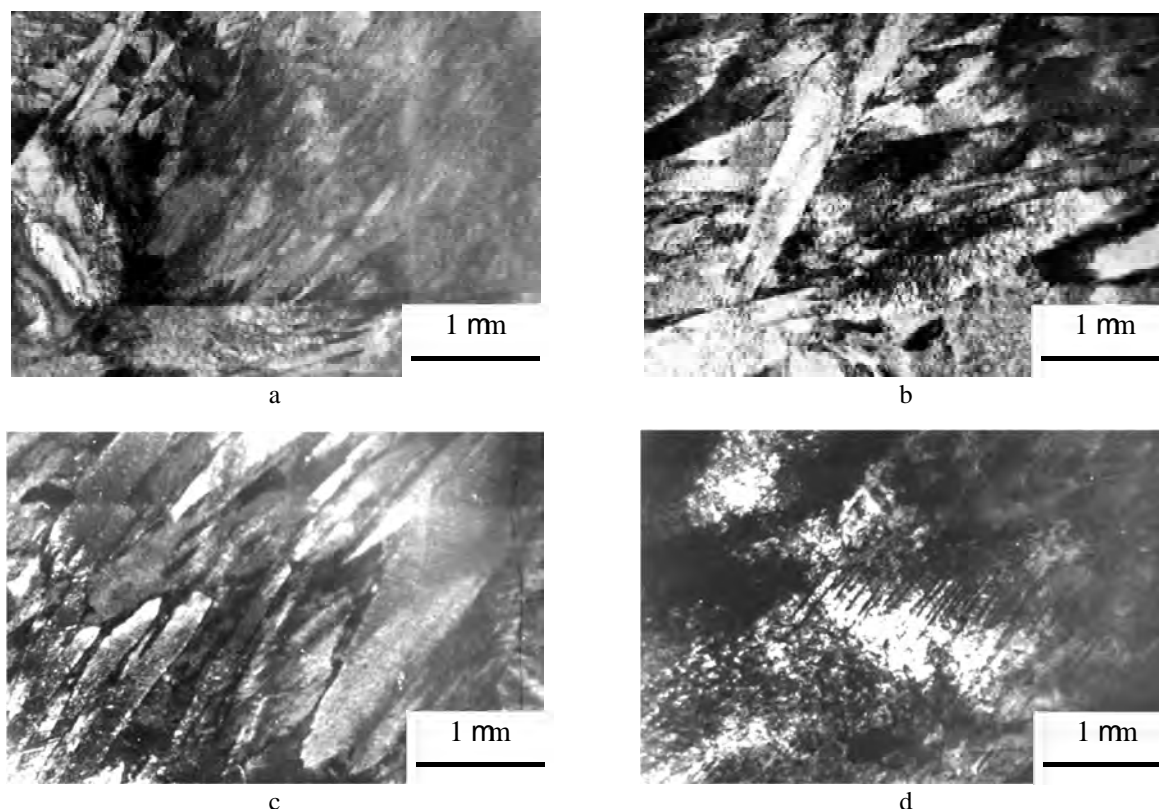


Fig. 7. The microstructure of 40Kh steel quenched from (a, b) 860 and (c, d) 1050 °C presenting (a, c) package- and (b, d) needle-shaped martensite

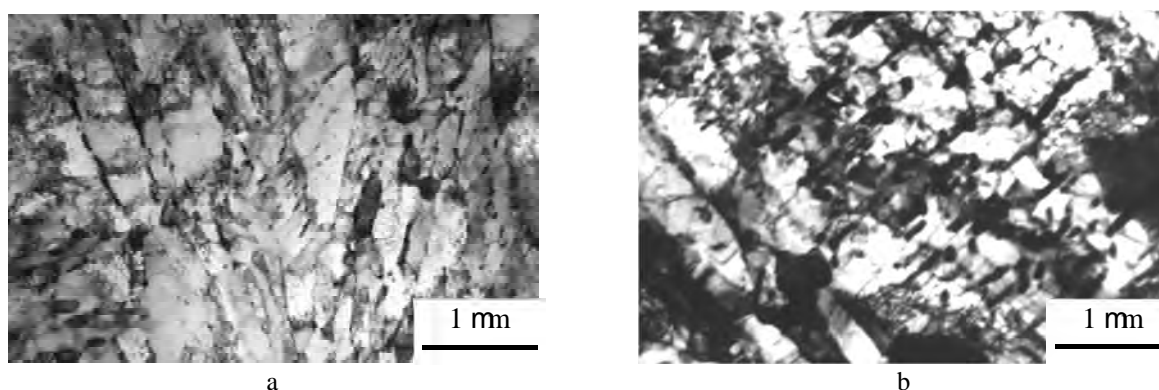


Fig. 8. The microstructure of 40Kh steel after quenching from 860 (a) and 1050 °C (b) and tempering at 600 °C

The structure of the vast majority of antifriction alloys is subject to the Sharpie-Bochvar principle [55, 56], according to which the hardest microstructural components should be uniformly distributed in the form of isolated sections in a less hard and ductile matrix [57–60]. The effectiveness of materials with such a structure is proven by years of experience in their use in moving joints [61]. Therefore, when developing new wear-resistant metallic materials or forming friction surfaces, it is advisable to create structures like a composite material, that is, contain hard particles distributed in a certain way in a

relatively soft matrix. Such particles can be, in particular, carbides of iron and alloying elements, complex carbides, and intermetallics [62].

The contact interaction during friction is accompanied by the processes of deformation and formation and destruction of frictional bonds in local areas of the surface, namely contact spots, the average diameter of which is 6–30 μm [63, 64]. Therefore, such an element of the microstructure, as the carbide phase, falls into the contact zone, and its behavior when applying external loads to varying degrees affects the resistance to contact fracture. At the end of the process of pre-working in the surface layer up to 10 μm thick, an oriented fragmented microstructure is formed. The process of normal friction and wear without burrs and grasp is determined by the formation and preservation of a stable structure within the contact spots, which can quasi-elastically accept the load. The stability of the structure within the spots is due to its resistance, as well as the equilibrium of supply and removal of defects at the fragment boundaries [64].

As carbides are numerous obstacles to the movement of dislocations and thus contribute to the high strength of steel, the carbide phase, its size, and mechanical properties play a special role in the process of increasing the wear resistance [65–68]. Therefore, the time of existence of the interaction spots will be determined, on the one hand, by the stability of the carbides with respect to their decomposition during plastic deformation, and on the other by the size of the carbides, on which the stability term during deformation depends [69–71].

The increasing non-uniformity of the carbon distribution in 40Kh steel with increasing the quenching temperature to 1050 $^{\circ}\text{C}$ contributes to the increase in the size of high-carbon crystals of needle-shaped martensite and the deposition of carbides stable to the decomposition during the plastic deformation. The last ones are deposited inside the martensite crystals at the microtwin boundaries during the tempering. They are larger than martensite packets. In this case, the friction surface becomes heterogeneous in mechanical properties due to the formation of separate sections, which can act as wear resistant contact spots and form the actual contact area. Therefore, the creation of a heterogeneous microstructure according to the Sharpie-Bochvar principle is one of the decisive factors in reducing the wear intensity of 40Kh steel.

The solution of specific materials science problems is based on the study of changes in the phase composition, microstructure and complex of mechanical properties depending on the operating conditions of the machine parts. Therefore, in addition to these internal factors, it is always necessary to take into account the temperature, pressure, presence or absence of lubricants, etc. These factors in the process of operation cause the transformation of the microstructure and stress state of the contact surfaces of the materials. In this case, the thermodynamic equilibrium is disturbed on the contacting surfaces, secondary structures are formed, selective dissolution of alloying elements, surface segregation, adsorption or desorption, reaction diffusion, etc. are also performed, which also affects the nature and mechanisms of tribological phenomena.

The course of the described processes can be regulated in different ways, in particular, by determining the types and morphology of the phases that would be appropriate to obtain at the contact surfaces, which will improve the tribological properties of moving joints [54, 72, 73]. To more precisely and diligently regulate the structure and phase composition of the surface layers of the investigated steel, which improve its tribological properties, the experimental data and computer simulation were combined. The solution of the tasks in the work requires consideration of many properties of materials. Therefore, it is advisable to use intelligent systems based on ANNs. Such systems are characterized by flexibility, and their functioning includes empirical, prediction-based skills.

In the work [74], using the values of quenching temperature ($t_{\text{rapr.}}$) and microhardness of contacting friction surfaces (H_{μ}) determined by sclerometer methods, the distance between their maximum values (T_2) and their average length (L_{cep}), and the average size of carbides ($D_{K_{\text{cep}}}$), a neural network was formed for prediction at $(i + 1)$ -th point according to the data of $(i - 1)$ -th and i -th points of three parameters (H_{μ} , T_2 , L_{cep}). But the ANN variant obtained was capable of modeling only interpolation points.

For modeling in both interpolation and extrapolation areas, the network architecture proposed in [74] and its teaching methodology were adapted. By applying the adapted ANN architecture (Fig. 9) due to the additional use of experimentally obtained values of the functional parameters of the surface Sr_1 and Sr_2 (Table 2), which characterize the function of the bearing capacity of the surface, tribological properties of 40Kh steel tempered after quenching from 860, 900, 950, 1050, 1160 and 1200 °C were predicted (Fig. 10). An analysis of the dynamics of changing the parameters Sr_1 and Sr_2 shows that raising the quenching temperature to 900 and 950 °C reduces the bearing capacity of the 40Kh steel specimens. Quenching from 1050 °C leads to an increase in the bearing capacity, and further temperature rise to 1160 and 1200 °C leads again to its decrease. The described changes in the functional parameters of the surface Sr_1 and Sr_2 obtained using the adapted ANN model, are similar to the simulation results reported in [74] and correlate with the results of wear resistance test of 40Kh steel obtained by the authors of the work [75].

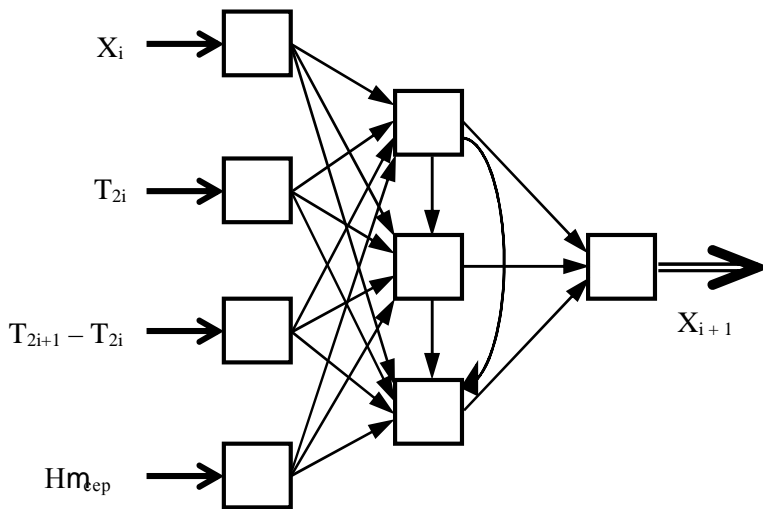


Fig. 9. Adapted neural network architecture: X_i is the surface parameter at the i -th scratch point; X_{i+1} is the surface parameter at the $i + 1$ scratch point; Hm_{ep} is the average value of microhardness; T_2 is the distance between extremes with maximum microhardness values

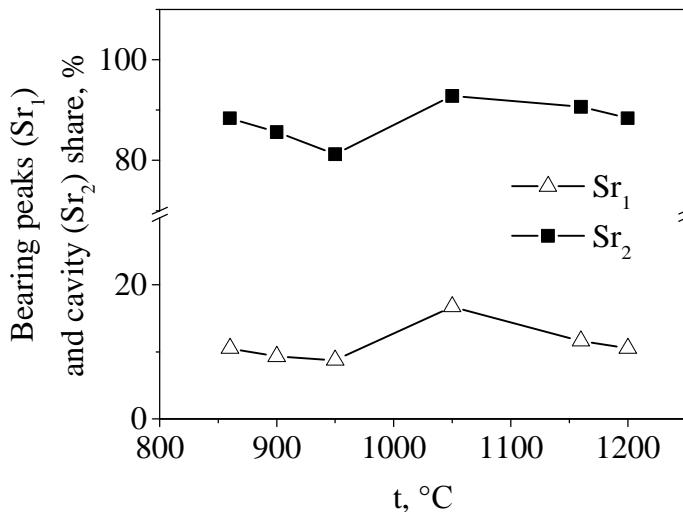


Fig. 10. Modeling and prediction of the functional parameters of the bearing capacity of the peaks (Sr_1) and valleys (Sr_2) on the 40Kh steel surface, depending on the quenching temperature (t)

Conclusions

It is found that the carbide phase morphology, which depends on the temperature conditions of heat treatment, affects the equilibrium roughness, structural-geometrical parameters, and bearing capacity of the 40Kh steel surface formed during contact interaction at friction, that, in turn, affects its tribological characteristics.

The architecture of the artificial neural network was adapted and the possibility of using neural network modeling to predict the change of structural-geometrical parameters characterizing the bearing capacity of the contact surfaces, depending on the quenching temperature of the investigated steel, was shown.

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According to the authors of the work, modeling using band calculations of the electronic structure [76, 77] of secondary structures that are formed during contact interaction and affect the tribological characteristics of materials, may also be promising.

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