

The Use of Combinatorial Methods for Sound Scanning of Objects

I. Tsmots¹, O. Riznyk², V. Rabyk³

¹Department of Automated Control Systems, Lviv Polytechnic National University,
28a, S. Bandery Str., 79008 Lviv, Ukraine; e-mail: ivan.tsmots@gmail.com

²Department of Publishing Information Technologies, Lviv Polytechnic National University,
28a, S. Bandery Str., 79008 Lviv, Ukraine; e-mail: ivan.tsmots@gmail.com

³Department of RadioPhysics and Computer Technologies, Ivan Franko National University of Lviv,
1, Universitetska, 79000 Lviv, Ukraine; e-mail: rabykv@ukr.net

Received October 31.2018: accepted November 01.2018

Abstract. In article considers application of combinatorial methods for research of sound images scan by the medium of integer sequences – ideal ring bundles as comfortable mathematical models for synthesis and optimization of systems with non-uniform structure. By using combinatorial approaches quality of methods based on the passage of sound signals through the tissues can be significantly improved. Studies show that the use of integer sequences based on the ideal ring bundles in information conversion tasks ensures simplicity of hardware application.

Key words: ideal ring bundle; non-uniform structure, sound diagnostic; sound generator; sound scanning.

INTRODUCTION

In recent years, more and more attention is paid to various methods of diagnostics in medicine: iridodiagnosis, nuclear magnetic resonance, echolocation, and others. First of all, you need to develop methods that do not affect the status of the object under investigation.

The value of each method depends on many parameters: objectivity, speed, accuracy. Secondary but also important parameters are the cost, mobility, independence of the method from the raw materials [1, 2, 5].

By using combinatorial approaches quality of methods based on the passage of sound signals through the tissues can be significantly improved. From our point of view, methods of sound probing are valuable also because they can be used not only in the field of medicine, but also in geology, construction, robotics and other industries [3, 4, 6].

FORMULATION OF THE PROBLEM

Let's consider the object, through which a sound wave is transmitted (Fig. 1). At point *A* it receives an audio signal that is represented as adding waves received from the acoustic conductor that is connected with sound generator. Since some cyclic pulse sequence arrives from the generator, then at the point *A* will be obtained the sum of these sequences, shifted by one time step [7, 10, 11].

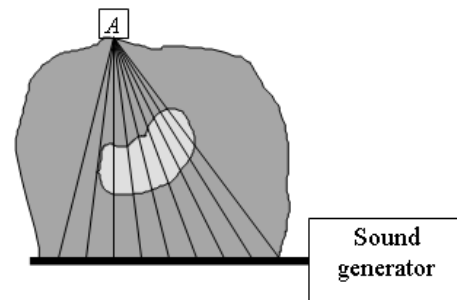


Fig. 1. Acoustic sounding scheme

In this case, if the damping of each wave path is different, and there is some sign on which at point *A* it is possible to distinguish the passage of the wave in each of the paths, then you can get information on the size of the acoustic noise that has encountered in each path.

Here, in this place, most of the existing algorithms assume a big mistake. The reliability of such implementation strongly depends on the nature of the distribution of the smallest significant bit in the container and in the message. And in the vast majority of cases, these distributions are different in different bits. And in pictures built using binary codes in the younger bits there will be roughly even distribution of “0” and “1”, and such an introduction will be noticeable even to the eye. Therefore, an important task is the choice of distribution of the smallest significant bit [8, 9, 12].

To solve the problem, it is first necessary to synthesize such a signal of the generator, which would differ in the shift [13, 15]. If you imagine a wave as $\{1, 0\}$ -sequence, then there are many such signals. If you select an arbitrary random signal length N of time steps, which, when shifting to step dt is not repeated, then the problem is reduced to the solution of the linear equation:

$$S \times X = F, \quad (1)$$

where S – is a matrix of size $N \times N$ signal $\{1, 0\}$, which is written in its first column. Each next column j of this matrix is cyclically shifted on j stacks down relative to the first column. X – matrix of attenuation size N , which characterizes the size of the acoustic noise in each direction of sound propagation, F is the matrix of the received signal at point A the size of N . If the reflection and external interference are not taken into account, then the signal received by the sensor, fixed in matrix F , should also be repeated cyclically.

Since equation (1) should be done for different points of the investigated object, the solutions of (1) must be present in the form of:

$$X = S^{-1} \times F, \tag{2}$$

where S is an inverse matrix. In this case if the problem is in the size of 1000 time steps (very few), the inverse matrix should be 1000×1000 , which firstly lead to unnecessarily high loss of memory, and the secondly will lose accuracy of calculations, since numerical methods require at least $N(N-1)$ multiplication and division operations.

Therefore, it is necessary to find such a kind of probing signal, which will allow to get analytical elements of the matrix S^{-1} and in addition, this expression for each of its elements should not be too complicated [16, 18].

SOLVING THE PROBLEM KEY

If, for the distance between the impulses of the probe signal, the ideal ring bundles of order M are chosen, then the value of $N = M(M-1)+1$ [19, 20, 29]. Ideal ring bundle is the set of positive integers, arranged as divisions on the ruler in the way that the distance between any two divisions is unique.

In other words, along the whole line, we cannot find two numbers with difference between them repeated twice [14, 23, 26].

The ideal ring bundle (IRB) is a sequence of $K_N = (k_1, k_2, \dots, k_N)$ numbers in which all possible circular sums exhaust the value from the row of natural numbers $1, 2, \dots, S_N$, where [14]:

$$S_N = N(N-1). \tag{3}$$

A binary code constructed in accordance with the ideal ring ratio $r(M)$ with a shift to any number of steps in the range from $[1, N(N-1)]$ has exactly one matching of units between the shifted and the initial combination [23, 24].

This property makes it possible to construct an inverse matrix based on such an algorithm:

- the matrix S is transposed;
- symbols $\{1\}$ are replaced by $1/M$;
- symbols $\{0\}$ are replaced by $(-1)/(M(M-1))$.

Consider, for example, the ideal ring bundle: 1, 3, 2, 7 [16, 17, 18]. With such parameters, the size of the matrix S will be: $N = 4 \times (4-1) + 1 = 13$. The cyclic signal generated by the generator should be: $\{1100101000000\}$, where the distance between impulses corresponds to the ideal ring ratio of 1, 3, 2, 7. By the given algorithm, the form of the matrices S and S^{-1} will be the following:

$$S = \begin{matrix} \begin{matrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 \end{matrix} \end{matrix}$$

In the following symbols $p = 1/4, k = -1/12$.

$$S^{-1} = \begin{matrix} \begin{matrix} p & p & k & k & p & k & p & k & k & k & k & k & k & k \\ k & p & p & k & k & p & k & p & k & k & k & k & k & k \\ k & k & p & p & k & k & p & k & p & k & k & k & k & k \\ k & k & k & k & p & p & k & k & p & k & p & k & k & k \\ k & k & k & k & k & p & p & k & k & p & k & p & k & p \\ p & k & k & k & k & k & p & p & k & k & p & k & p & k \\ k & p & k & k & k & k & k & p & p & k & k & p & k & p \\ p & k & p & k & k & k & k & k & p & k & p & k & k & k \\ k & p & k & p & k & k & k & k & k & k & p & p & k & k \\ k & k & p & k & p & k & k & k & k & k & k & p & p & p \\ p & k & k & p & k & p & k & k & k & k & k & k & p & p \end{matrix} \end{matrix}$$

Each element of the inverse matrix can be calculated from the cyclic sequence q , which is obtained from the sequence of the sound generator according to the above algorithm:

$$S_{ij}^{-1} = q_l, \tag{4}$$

where $q = p, p, k, k, p, k, p, k, k, k, k, k, k, k$ and $l = \text{mod } N(N+j-i)$.

Formally, the combinatorial properties of the codes underlying the matrices S and S^{-1} can be expressed as predicates over the lists in terms of logic of the 1st order.

The reproduction of the sound image, from our point of view, must take several steps:

- using the Figure 1 scheme, the fixation of audio signals at points located on the surface of the object is performed. This can be done by using the laws of laser wave interference, as it is done in holography;
- the received and recorded signals must be translated into the form of attenuation matrices in each direction of the propagation of acoustic waves. This step is reduced to the operation of

multiplication of matrices, (3) whose elements are calculated by the formula (4);

- matrix of attenuation must be transformed into a matrix $\{x_{ijk}\}$ of the structure of the object itself. This step is the most time-consuming and requires some assumptions which will be discussed further;
- the last step is the visualization of the image on the screen of your computer, which in itself is a separate engineering problem that we won't investigate.

For transformation of sound signal attenuation matrices in a matrix structure against of the object let's consider the scheme of sound waves routing, shown in Fig. 2.

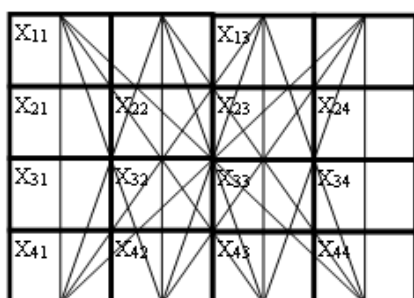


Fig. 2. A chart of passing of acoustic waves is through the object of cellular structure

To solve the problem, one must make the following assumptions:

- the object has a cell structure;
- fading factor $\{x_{ijk}\}$ of acoustic signals in the cell (i, j, k) is constant for the whole cell;
- each cell is a parallelepiped.

According to the latest assumption, the attenuation of the energy of each beam passing through the cell at an arbitrary angle is proportional to the length of the segment that is cut off at the beam by the edges of the cell.

Thus, if each cell is a parallelepiped, then the measuring scheme “automatically” sets the matrix of the lengths of the rays L in the middle of each cell [27, 28, 30].

As can be seen from Fig. 2, the number of cells should be equal to the number of equations. Only in this case one can find the absorption factor of each cell [21, 22, 25].

CONCLUSIONS

During implementation works were the collected and studied materials about technologies of voice scan-out of objects by means of ideal ring bundles.

A practical value the got results will allow optimally to choose the signal of voice generator which will provide more effective work of devices of voice scan-out.

REFERENCES

1. **A. G. Holubnychi and G. F. Konakhovych**, “Spread-spectrum control channels for UAV based on the generalized binary Barker sequences”, 2013 IEEE 2nd International Conference Actual Problems of Unmanned Air Vehicles Developments Proceedings (APUAVD), Kiev, 2013, pp. 99–103. doi: 10.1109/APUAVD.2013.6705296.
2. **C. R. Lakshmi, D. Trivikramarao, S. Subhani and V. S. Ghali**, “Barker coded thermal wave imaging for anomaly detection”, 2018 Conference on Signal Processing And Communication Engineering Systems (SPACES), Vijayawada, India, 2018, pp. 198–201. doi: 10.1109/SPACES.2018.8316345.
3. **C. Rusu and J. Thompson**, “On the use of tight frames for optimal sensor placement in time-difference of arrival localization”, 2017 25th European Signal Processing Conference (EUSIPCO), Kos, 2017, pp. 1415–1419. doi: 10.23919/EUSIPCO.2017.8081442.
4. **G. Dua and R. Mulaveesala**, “Applications of barker coded infrared imaging method for characterisation of glass fibre reinforced plastic materials”, in Electronics Letters, vol. 49, no. 17, pp. 1071–1073, August 15 2013. doi: 10.1049/el.2013.1661.
5. **H. Bae, J. Kim and J. Burm**, “The enhancement of Signal-to-Noise Ratio of SAW tags using 5-bit Barker code sequence”, The 40th European Microwave Conference, Paris, 2010, pp. 49–52. doi: 10.23919/EUMC.2010.5616316.
6. **I. Tsmots, O. Berezkyi, I. Ihnatiev and I. Gumovska**, “Implementation of image processing algorithms based on GPU”, 2016 XIth International Scientific and Technical Conference Computer Sciences and Information Technologies (CSIT), Lviv, 2016, pp. 27–29. doi: 10.1109/STC-CSIT.2016.7589860.
7. **J. Fu, G. Wei and Q. Huang**, “Barker coded excitation using LFM carrier for improving axial resolution in ultrasound imaging”, 2013 ICME International Conference on Complex Medical Engineering, Beijing, 2013, pp. 150–153. doi: 10.1109/ICCME.2013.6548229.
8. **J. Kaur and G. Kaur** “An amended ant colony optimization based approach for optimal route path discovery in wireless sensor network”, 2017 IEEE International Conference on Smart Technologies and Management for Computing, Communication, Controls, Energy and Materials (ICSTM), Chennai, 2017, pp. 353–357. doi: 10.1109/ICSTM.2017.8089184.
9. **J. S. Jeong**, “Suppression of therapeutic interference by using Barker code and adaptive notch filtering for real-time HIFU surgery and ultrasound imaging”, in Electronics Letters, vol. 49, no. 14, pp. 871–873, July 4 2013. doi: 10.1049/el.2013.0418.
10. **J. Soba, A. Munir and A. B. Suksmo**, “Barker code radar simulation for target range detection using software defined radio”, 2013 International Conference on Information Technology and Electrical Engineering (ICITEE), Yogyakarta, 2013, pp. 271–276. doi: 10.1109/ICITEE.2013.6676251.

11. **J. Zhu et al.**, "Detection of scatters motion induced by mechanical vibrator using 7-chip barker-coded excitation", 2014 7th International Conference on Biomedical Engineering and Informatics, Dalian, 2014, pp. 51–55. doi: 10.1109/BMEI.2014.7002741.
12. **M. Kellman, F. Rivest, A. Pechacek, L. Sohn and M. Lustig**, "Barker-Coded node-pore resistive pulse sensing with built-in coincidence correction", 2017 IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP), New Orleans, LA, 2017, pp. 1053–1057. doi: 10.1109/ICASSP.2017.7952317.
13. **N. Liu and C. Peng**, "Barker and m-Sequence Auto-Correlation Reception", 2009 First International Conference on Information Science and Engineering, Nanjing, 2009, pp. 2563–2565. doi: 10.1109/ICISE.2009.359.
14. **O. Riznyk, I. Yurchak, E. Vdovenko and A. Korchagina**, "Model of stegosystem images on the basis of pseudonoise codes", 2010 Proceedings of Vth International Conference on Perspective Technologies and Methods in MEMS Design, Lviv, 2010, pp. 51–52.
15. **O. Riznyk, B. Balych and I. Yurchak**, "A synthesis of barker sequences is by means of numerical bundles", 2017 14th International Conference The Experience of Designing and Application of CAD Systems in Microelectronics (CADSM), Lviv, 2017, pp. 82–84. doi: 10.1109/CADSM.2017.7916090.
16. **O. Riznyk, I. Yurchak and O. Povshuk**, "Synthesis of optimal recovery systems in distributed computing using ideal ring bundles", 2016 XII International Conference on Perspective Technologies and Methods in MEMS Design (MEMSTECH), Lviv, 2016, pp. 220–222. doi: 10.1109/MEMSTECH.2016.7507545.
17. **O. Riznyk, V. Parubchak and D. Skybajlo-Leskiv**, "Information Encoding Method of Combinatorial Configuration", 2007 9th International Conference – The Experience of Designing and Applications of CAD Systems in Microelectronics, Lviv-Polyana, 2007, pp. 370–370. doi: 10.1109/CADSM.2007.4297583.
18. **O. Riznyk, Y. Kynash, O. Povshuk and V. Kovalyk**, "Recovery schemes for distributed computing based on BIB-schemes", 2016 IEEE First International Conference on Data Stream Mining & Processing (DSMP), Lviv, 2016, pp. 134–137. doi: 10.1109/DSMP.2016.7583524.
19. **P. Kaczmarek, T. Mańkowski and J. Tomczyński**, "Towards sensor position-invariant hand gesture recognition using a mechanomyographic interface", 2017 Signal Processing: Algorithms, Architectures, Arrangements, and Applications (SPA), Poznan, 2017, pp. 53–58. doi: 10.23919/SPA.2017.8166837.
20. **Pilsu Kim, Eunji Jung, Sua Bae, Kangsik Kim and Tai-kyong Song**, "Barker-sequence-modulated golay coded excitation technique for ultrasound imaging", 2016 IEEE International Ultrasonics Symposium (IUS), Tours, 2016, pp. 1–4. doi: 10.1109/ULTSYM.2016.7728737.
21. **R. C. Nilawar and D. M. Bhalerao**, "Reduction of SFD bits of WiFi OFDM frame using wobulation echo signal and barker code", 2015 International Conference on Pervasive Computing (ICPC), Pune, 2015, pp. 1–3. doi: 10.1109/PERVASIVE.2015.7087095.
22. **R. M. Ford, R. S. Weissbach and D. R. Loker**, "A DSP-based modified Costas receiver for LVDT position sensors", Proceedings of the 17th IEEE Instrumentation and Measurement Technology Conference [Cat. No. 00CH37066], Baltimore, MD, 2000, pp. 1448–1452 vol.3. doi: 10.1109/IMTC.2000.848714.
23. **R. Oleg, K. Yurii, P. Oleksandr and B. Bohdan**, "Information technologies of optimization of structures of the systems are on the basis of combinatorics methods", 2017 12th International Scientific and Technical Conference on Computer Sciences and Information Technologies (CSIT), Lviv, 2017, pp. 232–235. doi: 10.1109/STC-CSIT.2017.8098776.
24. **S. König, M. Schmidt and C. Hoene**, "Precise time of flight measurements in IEEE 802.11 networks by cross-correlating the sampled signal with a continuous Barker code", The 7th IEEE International Conference on Mobile Ad-hoc and Sensor Systems (IEEE MASS 2010), San Francisco, CA, 2010, pp. 642–649. doi: 10.1109/MASS.2010.5663785.
25. **S. M. Omar, F. Kassem, R. Mitri, H. Hijazi and M. Saleh**, "A novel barker code algorithm for resolving range ambiguity in high PRF radars", 2015 European Radar Conference (EuRAD), Paris, 2015, pp. 81–84. doi: 10.1109/EuRAD.2015.7346242.
26. **S. R. Blackburn and T. Etzion**, "PIR array codes with optimal PIR rates", 2017 IEEE International Symposium on Information Theory (ISIT), Aachen, 2017, pp. 2658–2662. doi: 10.1109/ISIT.2017.8007011.
27. **S. R. Blackburn, T. Etzion, K. M. Martin and M. B. Paterson**, "Distinct Difference Configurations: Multihop Paths and Key Predistribution in Sensor Networks", in IEEE Transactions on Information Theory, vol. 56, no. 8, pp. 3961–3972, Aug. 2010. doi: 10.1109/TIT.2010.2050794.
28. **Siti Julia Rosli, Hasliza Rahim, Ruzelita Ngadiran, K. N. Abdul Rani, Muhammad Imran Ahmad and Wee**, "Design of Binary Coded Pulse Trains with Good Autocorrelation Properties for Radar Communications", 2018 MATEC Web of Conferences, doi: 10.1051/mateconf/201815006016.
29. **V. Riznyk, O. Riznyk, B. Balych and V. Parubchak**, "Information Encoding Method of Combinatorial Optimization", 2006 International Conference – Modern Problems of Radio Engineering, Telecommunications, and Computer Science, Lviv-Slavsko, 2006, pp. 357–357. doi: 10.1109/TCSET.2006.4404550.
30. **Y. Chunhong and L. Zengli**, "The Superiority Analysis of Linear Frequency Modulation and Barker Code Composite Radar Signal", 2013 Ninth International Conference on Computational Intelligence and Security, Leshan, 2013, pp. 182–184. doi: 10.1109/CIS.2013.45.