

Recurrence plots parameters during epileptic seizure patterns onset

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Abstract – The purpose of the paper is to investigate the applicability of recurrence plots parameters for early detection of epileptic seizures. Trends of Recurrence Rate and Determinism of electroencephalogram recurrence plots are calculated for different time windows. Experiments show that both parameters start to grow approximately 250 seconds in advance of epileptic seizure activity onset for time window of 5 minutes.

Key words – epilepsy, seizure prediction, recurrence plots.

I. Introduction

Epilepsy is one of the most common neurologic disorders worldwide. It is characterized by repeated unpredictable seizures caused by excessive abnormal synchronous activity of neuronal groups in the brain. Clinical manifestations of epilepsy are unforeseen and abrupt motor phenomena, loss of consciousness, psychic and sensory symptoms etc., causing the low everyday life quality of sufferers. Despite the availability of variety of antiepileptic drugs, one third of patients have intractable seizures. Due to this fact, the need for automated techniques for epileptic seizures prediction and control is of great interest [1]. The most widespread way to analyze brain functioning in healthy and epileptic conditions is to apply various signal analysis techniques to the electroencephalogram (EEG) signal.

This paper is aimed to demonstrate the application of EEG recurrence plots analysis to the prediction of seizure onset.

II. Detection of epileptic patterns using recurrence plots

Recurrence plot (RP) is the graphical tool allowing to explore the m -dimensional phase space trajectory of the nonlinear system through a two-dimensional representation of its recurrence and, therefore, to see a dynamic picture. This approach was introduced in [2, 3] and is used in the investigations of nonlinear systems parameters and behavior.

Let point $x(i)$ corresponds to i -th point of the phase trajectory ($i = 1 \dots N$) describing dynamical system in m -dimensional space. Then recurrence plot for this system is an array of $N \times N$ elements, where a nonzero element with the coordinates (i, j) corresponds to the case when $x(i)$ is sufficiently close to $x(j)$.

The closeness between different point in phase space is usually depicted by the black and white points on the recurrence picture, where black color corresponds to the presence of recurrence (closeness of system states in

phase space) and white color means that the states of the system are significantly different. Recurrence of the states is defined by

$$R_{j,i} = \theta(\varepsilon_i - \|x(i) - x(j)\|),$$

where $x(i) \in L^m$, $i, j = 1 \dots N$, ε_i – minimal distance between points interpreted as a radius of m -dimensional sphere around the points in phase space, $\|\cdot\|$ – norm, $\theta(\cdot)$ – Heaviside step function.

To characterize the system behaviour a number of recurrence plots parameters are proposed, see e.g. [4-6]. They are used to go beyond visual inspection of the plots and to measure the complexity of underlying system. In this paper the following are used to study possibility of epileptic seizures pattern prediction:

– Recurrence rate

$$RR = \frac{1}{N^2} \sum_{i,j=1}^N R_{i,j}^{m,\varepsilon};$$

– Determinism of the system

$$DET = \frac{\sum_{l=l_{\min}}^N IP(\varepsilon, l)}{\sum_{l=1}^N IP(\varepsilon, l)},$$

where

$$P(\varepsilon, l) = \sum_{i,j=1}^N (1 - R_{i-1,j-1}(\varepsilon))(1 - R_{i+1,j+1}(\varepsilon)) \prod_{k=0}^{l-1} R_{i+k,j+k}(\varepsilon).$$

The aim of experimental part is to investigate the applicability of recurrence plots parameters for early detection of epileptic seizures. Example of one EEG channel containing burst of seizure activity is given in Fig.1. Seizure is started after 1850 second on this figure and characterized by the change in EEG magnitude without significant alternation of oscillatory behavior. The onset of seizure activity should be predicted as early as possible before changes.

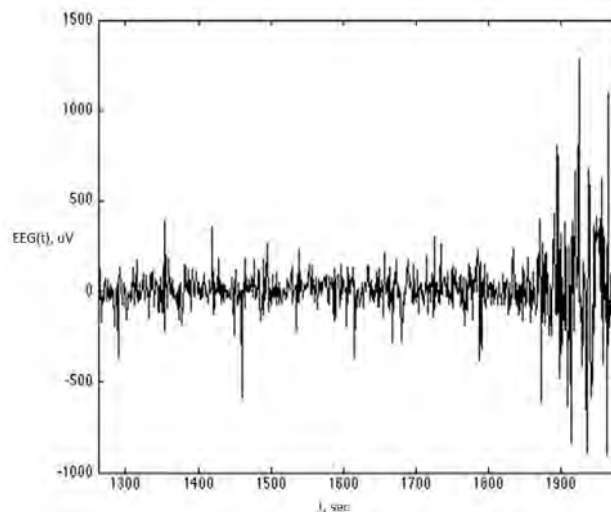


Fig. 1. Part of one EEG channel with seizure activity

III. Experimental Results

The main idea of the presented work is to find out if the chosen RP parameters change their value prior to the seizure onset. For this purpose the EEG signals containing epileptic patterns were selected from public available database [7].

To study the RP parameters trends, several time windows were chosen (durations from 1 second to 5 minutes) and RP parameters were calculated in sliding windows. Resulting plots are given in Fig. 2-3 for window duration of 1 second, and for 5 min. window.

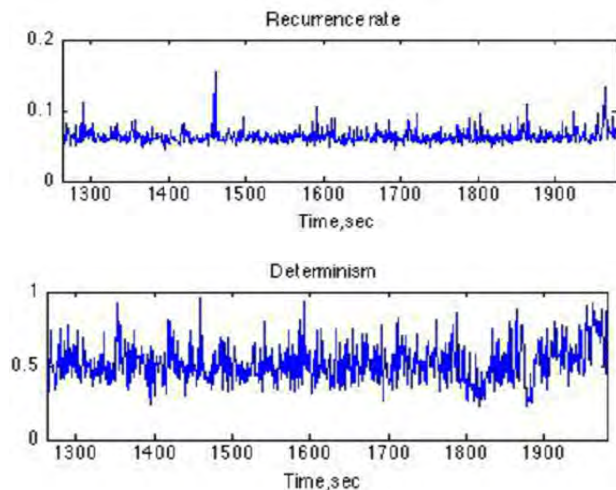


Fig. 2. RP parameters for window of 1 sec duration

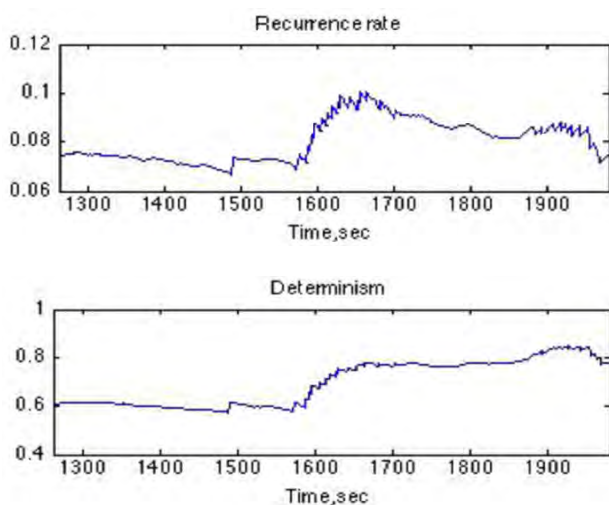


Fig. 3. RP parameters for window of 5 minutes duration

It can be seen that depending on the time window duration, the trends of the parameters value are different. In case of 1 sec. there is no change in parameters neither before seizure nor during seizure. The behavior is the

same for both recurrence rate and determinism, thus these parameters cannot be used for prediction and even for detection of seizure onset.

The opposite behaviour occurs for the case when time window is 5 minutes. There are prominent changes in RP parameters values for both recurrence rate and determinism: they start to grow approximately 250 seconds in advance of seizure onset and keep large up to the seizure time. This time period is sufficient to forestall the epileptic seizure.

The drawback in this approach is significant time for calculations of RP parameters, thus further research is needed to adjust recurrence plots parameters calculation procedure and investigate other parameters feasible for epileptic seizure prediction.

Conclusion

In this paper recurrence plots of EEG signals containing epileptic patterns were obtained and their parameters were calculated in sliding time window during background activity and seizure onset. It is shown that some parameters, namely recurrence rate and determinism of recurrence plots have changed drastically prior to the seizure onset and thus are promising for epileptic seizures prediction.

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